



$u_k \sim \text{i.i.d.}$

$y_k = \sum_{i=0}^{\infty} \delta_i \mu(u_{k-i}) + z_k$

H

$$R(u) \triangleq E\{y_k \mid u_k = u\} = E\left\{ \delta_0 \mu(u_k) + \sum_{i=1}^{\infty} \delta_i \mu(u_{k-i}) + z_k \mid u_k = u \right\} =$$

$$= \delta_0 \mu(u) + \underbrace{c_1}_{\text{const.}}$$

$$c_1 = \bar{w} \cdot \sum_{i=1}^{\infty} \delta_i$$

$$R(u^{(1)}, u^{(2)}) = E\{y_k \mid u_k = u^{(1)} \text{ AND } u_{k-1} = u^{(2)}\} =$$

$$= E\left\{ \delta_0 \mu(u_k) + \delta_1 \mu(u_{k-1}) + \sum_{i=2}^{\infty} \delta_i \mu(u_{k-i}) + z_k \mid \dots \right\} =$$

$$= \delta_0 \mu(u^{(1)}) + \delta_1 \mu(u^{(2)}) + c_2$$

$$c_2 = \bar{w} \cdot \sum_{i=2}^{\infty} \delta_i$$

$$R\left(u^{(1)}, u^{(2)}, \dots, u^{(L)}\right) = [\delta_0, \dots, \delta_{L-1}] \begin{bmatrix} \mu(u^{(1)}) \\ \vdots \\ \mu(u^{(L-1)}) \end{bmatrix} + c_L$$

$\mu(\cdot) = \alpha_1 \varphi_1(\cdot) + \dots + \alpha_S \varphi_S(\cdot)$

$$c_L = \bar{w} \cdot \sum_{i=L}^{\infty} \delta_i$$

if the L objed: FIR(L)

$\underbrace{\delta_L, \delta_{L+1}, \dots}_{=0} \Rightarrow c_L = 0$