



$\theta_1, \theta_2, \dots, \theta_k, \dots, \theta_N$

gives

$$Q(\theta) = \sum_{k=1}^N w_k (\theta - \theta_k)^2 \rightarrow \min_{\theta}$$

$$\frac{\partial Q(\theta)}{\partial \theta} = \sum_{k=1}^N 2w_k (\theta - \theta_k) = 0 \quad / : 2$$

$$\sum_{k=1}^N w_k (\theta - \theta_k) = 0$$

$$\sum_{k=1}^N \theta = \sum_{k=1}^N \theta_k$$

$$N\theta = \sum_{k=1}^N \theta_k \quad / : N$$

$$\theta = \frac{1}{N} \sum_{k=1}^N \theta_k$$

spread case  
 $w_k = 1$

$$\sum_{k=1}^N w_k \theta = \sum_{k=1}^N w_k \theta_k$$

$$\theta \sum_{k=1}^N w_k = \sum_{k=1}^N w_k \theta_k$$

$$\theta = \frac{\sum_{k=1}^N w_k \theta_k}{\sum_{k=1}^N w_k}$$

$$w_k = 1$$

weighted mean

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